

**Recitation #9**  
**Quantum 522**

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1. Consider scattering of a potential  $V(r) = -V_0\theta(r_0 - r)$ . In the Born approximation, find the total cross section in the limit  $kr_0 \rightarrow 0$  and show that it is isotropic. With  $q = 2k \sin(\theta/2)$  the Born approximation is

$$f^{(1)}(\theta) = \frac{-2m}{q\hbar^2} \int_0^\infty r \sin(qr) V(r) dr$$

2. Calculate the total cross section for scattering off of a Yukawa potential. In class we found (with  $m_0 = 1/r_0$ )

$$\frac{d\sigma}{d\Omega} = \left( \frac{2mg}{\hbar^2} \right)^2 \left( \frac{r_0^2}{q^2 r_0^2 + 1} \right)^2$$

Hint:  $q^2 = 2k^2(1 - \cos \theta)$  and change variables from  $\cos \theta$  to  $q^2$ .

Take the limit  $r_0 \rightarrow \infty$ . What is the total Rutherford cross section?