

**Intermediate Quantum 492: HW #7 Extra**

Spectroscopic Term and Hund's Rules

Determine the spectroscopic term for the ground state of Carbon. First, make a table of all possible values of  $\ell$ ,  $s$  and  $j$ . Include a column for the symmetry of the spatial part and the spin part as  $\pm$ . Eliminate the rows of the table that are excluded by the Pauli principle. Add a column for the spectroscopic term  $^{2S+1}L_J$  for all Pauli allowed rows. Finally, apply Hund's rules to determine the ground state.

You can get the same result using a short-cut (from Gasiorowicz). Make a drawing with horizontal lines ("shelves") corresponding to the values of  $m_\ell$  for the  $L$  of the sub-shell. Distribute the electrons as up or down arrows on the shelves, only doubling up on an  $m_\ell$  when necessary and using Hund's rule 1 to maximize the sum of  $s_z$  which gives  $S$ . Sum the  $m_\ell$  for the shelves to get  $L$  as  $L = \sum n_i \cdot m_i$  where  $n_i$  is the number of electrons on the shelf. Use Hund's rule 3 to give  $J$ . For Carbon the diagram would be,

$$\begin{array}{l}
 m=1 \quad \text{---} \uparrow \\
 m=0 \quad \text{---} \uparrow \\
 m=-1 \quad \text{---} \\
 \\
 S = 1/2+1/2=1 \\
 L = \sum n_i \cdot m_i = 1(1)+1(0)+0(-1) = 1
 \end{array}$$

Use this technique to find the spectroscopic term for oxygen and manganese.