

HW #7 Problems
Quantum 521

1. Solve the double delta-function potential and obtain the even and odd parity energy eigenstates.

$$V(x) = -V_0 [\delta(x - a) + \delta(x + a)]$$

For what value of V_0 does only the ground state exist?

In the limit $mV_0a \gg \hbar^2$ find the binding energies. Explain physically why the binding energies become close together as a goes to infinity.

2. Consider the one-dimensional scattering of a particle of mass m and energy $E > 0$ off of an arbitrarily shaped potential barrier $V(x)$ that is non-zero only in the interval $0 < x < a$. Prove that the transmission coefficient is the same whether the particle is incident on the barrier from the left or the right.
3. Find the uncertainty product $\Delta x \Delta p$ for the simple harmonic oscillator for all states $|n\rangle$.
4. Calculate the time evolution of $\langle x \rangle$ and $\langle p \rangle$ for the simple harmonic oscillator.
5. Prove that the parity operator for the one dimensional simple harmonic oscillator is $\hat{P} = \exp(i\pi\hat{N})$ where \hat{N} is the number operator.
6. Consider a charged particle $-q$ in a one dimensional harmonic oscillator $V(x)$ with a constant electric field \mathcal{E} in the x -direction. Find the energy eigenvalues. Find the energy eigenvectors.
7. For the ammonia molecule take the state at $t = 0$ to be $|\psi(0)\rangle = |1\rangle$. Calculate the probability as a function of time for the molecule to be in state $|1\rangle$.