

Recitation #4
Quantum 521

1. Prove that if an operator is skew hermitian $A^\dagger = -A$ that it can have only one real eigenvalue.
2. In the notation from class, for hermitian operators A, B defining $A' \equiv A - \langle A \rangle$ and similarly for B' show that if $A'|\psi\rangle = cB'|\psi\rangle$ and the anticommutator $\{A, B\} = 0$ that

$$\Delta A \Delta B = |\langle [A, B] \rangle|/2$$

(minimum uncertainty product). What kind of constant is c ?

For the Gaussian plane wave state with momentum $\hbar k$ find the constant c .

$$\Psi(x) = \alpha \exp\left\{ikx - \frac{x^2}{4\sigma^2}\right\}$$

where α is the normalization constant.